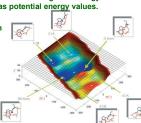
The use of quantum chemistry **Definitions**

- The purpose of quantum chemistry is to determine the equilibrium geometries of molecules.
- eimer approximation: the assumption that the motion
- of atomic nuclei and electrons in a molecule can be separated.

 Potential energy surface (PES): We can assign the energy of electrons to space coordinates as potential energy values.

• A PES describes the energy of a system (especially a collection of atoms) in terms of certain parameters, normally the positions of the atoms

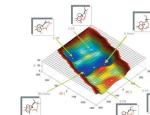


The use of quantum chemistry **Chemically important points of PES**

Minima

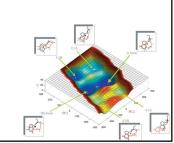
- The individual molecules, stable conformers can be assigned to them.

- First derivatives (gradients) are 0, second derivatives are positive.
 There are global and local minima.
 The "depth" of the minima sets the relative thermodynamic stability of each molecule/conformer.



The use of quantum chemistry Chemically important points of PES

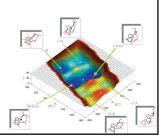
Saddle points
Gradients are 0, second derivatives are negative except for one.



The use of quantum chemistry Chemically important points of PES

<u>Maxima</u>

First derivatives (gradients) are 0, second derivatives are negative.



The use of quantum chemistry **Calculation methods**

- Molecular mechanics:

 The interactions between atoms are described with classical mechanical potentials.
- Due to its speed, large systems can be described and it is suitable for large-scale computation (biological systems, molecular dynamics). However, the results provided are relatively inaccurate.
- · Unsuitable for examining electronic structure.

Hartree-Fock method:

A method developed to solve the non-relativistic Schrödinger equation • Equations using the Born-Oppenheimer approximation (separation of atomic nuclei and electron movements) and the single electron

approximation (separation of single electron movements) are solved by the variational method/principle.

Base: Functions used to decompose the wave function.

The individual atomic orbital functions of the LCAO series expansion are usually constructed from Gaussian functions. Base 3-21G* denotes the electron orbitals within the core of the atom, it consists of 3 Gaussian functions (with constant coefficients),. The electron orbitals on the valence shell are constructed from eparate functions composed of 2 or 1 Gaussian functions)

The use of quantum chemistry **Calculation methods**

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emiempirical calculations

By neglecting and/or substituting some of the integrals that occur during the HF method with experimental values, we can make faster but more inaccurate calculations.

The use of quantum chemistry **Calculation methods**

- Molecular mechanics:
 The interactions between atoms are described with classical mechanical potentials.
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- A method developed to solve the non-relativistic Schrödinger equation
 Equations using the Born-Oppenheimer approximation (separation of atomic nuclei and electron movements) and the single electron approximation (separation of single electron movements) are solved by the variational method/principle.

ost-HE calculation

- These are methods for taking into account the effects neglected by the oneelectron approach (such as electron correlation).
- Their calculation costs are significantly higher than those for the HF method.

The use of quantum chemistry **Calculation methods**

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- Due to its speed, large systems can be described and it is suitable for large-scale computation (biological systems, molecular dynamics). However, the results provided are relatively inaccurate.
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- A method developed to solve the non-relativistic Schrödinger equation.
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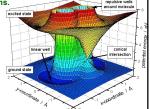
DFT (Density Functional Theory):

- Instead of the wave function, it uses the electron density to calculate the characteristics of the chemical system.
- The cost of DFT calculations (processor time, memory, data storage) is similar to HF calculations but gives better results.

The use of quantum chemistry Some computable properties

- Energy:

 Total energy according to the applied method, base, atomic coordinate (geometry) and electron state.
- · Its value itself is not useful for many, but when plotted against the coordinates of the atomic nuclei, it is possible to draw the PES where the energy differences between the individual points provide data for modeling chemical transformations.
- Energy differences of PES's of the same atomic nucleus configurations but different electron states give information about the excitation process.



The use of quantum chemistry Some computable properties

- Coordinate set for a well-defined point (minimum, saddle, ...) of a given
- PES (e.g. bond angles, bond distances, di-angular angles).

 Equilibrium geometry: coordinates belonging to a (local or global)
- minimum. Steps of geometry optimization:

choosing a starting geometry calculation of energy calculation of gradients change geometry in the direction of the gradient

calculation of energy again
(if the change of energy and gradients is small enough, STOP)

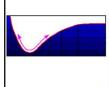


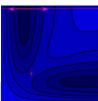
The use of quantum chemistry Some computable properties

Vibrations:

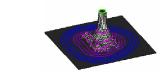
- Assuming harmonic oscillations, the second derivatives of the PES against spatial coordinates (force constants) can be used to calculate the frequencies of the molecular vibrations.

 In addition to characterizing a given point of the PES, they are also
- suitable for determining the partition function (i.e. thermodynamic properties can be calculated).







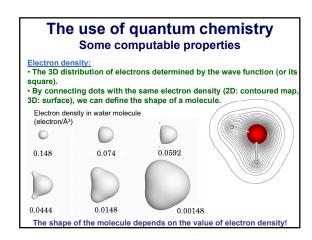


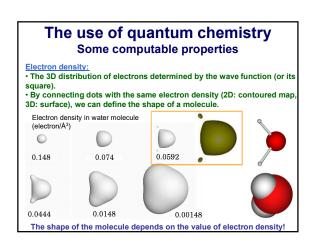


The use of quantum chemistry Some computable properties

Electron density:

- The 3D distribution of electrons determined by the wave function (or its
- By connecting dots with the same electron density (2D: contoured map 3D: surface), we can define the shape of a molecule.



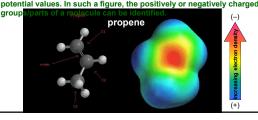


The use of quantum chemistry Some computable properties

- Electron density:
 The 3D distribution of electrons determined by the wave function (or its
- · By connecting dots with the same electron density (2D: contoured map 3D: surface), we can define the shape of a molecule.
- The points of such a surface can be colored based on their electrostati potential values. In such a figure, the positively or negatively charged groups/parts of a molecule can be identified.

The use of quantum chemistry Some computable properties

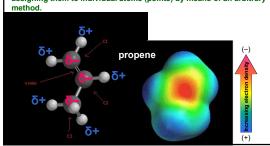
- Electron density:
 The 3D distribution of electrons determined by the wave function (or its
- · By connecting dots with the same electron density (2D: contoured map. 3D: surface), we can define the shape of a molecule
- · The points of such a surface can be colored based on their electrostation potential values. In such a figure, the positively or negatively charged



The use of quantum chemistry Some computable properties

Atomic charges:

• Determining the values of electron densities (3D distribution) and assigning them to individual atoms (points) by means of an arbitrary



Structures of molecules

- Born-Oppenheimer approximation: the assumption that the motion
- of atomic nuclei and electrons in a molecule can be separated.

 Potential energy surface (PES): We can assign the energy of electrons to space coordinates as potential energy values

The contribution of the vibration

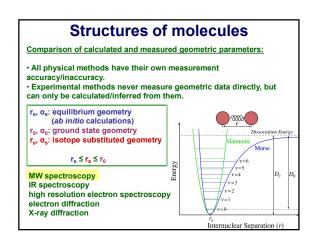


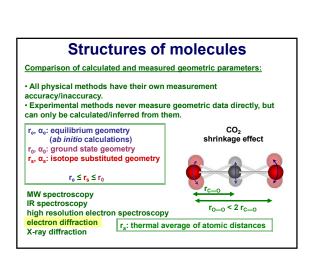
The goal is to find the geometric parameters for which the electron energy is minimal.

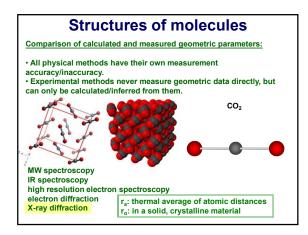
In addition to the Schrödinger equation for electrons, the Schrödinger equation for the vibrations of the atomic nuclei must also be solved...

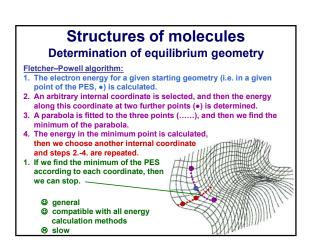


Until today, only for molecules containing a few atoms have succeeded









Structures of molecules **Determination of equilibrium geometry**

Gradient method:

There are many different algorithms, but they have the same principle: • The 1st and 2nd derivatives of the energy coordinates give the gradient vector (the magnitude of the force in a given direction) and the Hess matrix (force constants).

Elements of gradient vector:
$$F_{\rm ix} = -\left(\frac{{
m d}E}{{
m d}x}\right)_{{
m x}={
m x}}$$

Elements of Hess matrix:
$$H_{\mathrm{ixz}} = \left(\frac{\mathrm{d}^2 E}{\mathrm{d}x\mathrm{d}z}\right)_{x=x_{\mathrm{i}},z=z_{\mathrm{i}}}$$

Structures of molecules **Determination of equilibrium geometry**

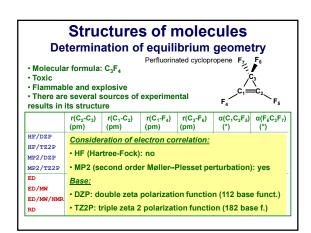
Gradient method:

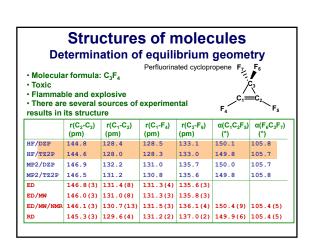
There are many different algorithms, but they have the same principle:
• The 1st and 2nd derivatives of the energy coordinates give the gradient vector (the magnitude of the force in a given direction) and the Hess matrix (force constants).

- We pick a point near the presumed minimum on PES.
- We are looking for the steepest slope and take a step in this direction
 PES is approximateed with parabola toward the gradient. The size of
- the next step is chosen to reach the minimum of the parabola.

 4. E and the gradient is calculated in the new point and we take a step
- again to F (use of the Hess matrix is advisable).

 5. If each element of the gradient vector is less than a predetermined threshold, and when all of the force constants are positive, then we
 - fast (analytical differentiation can be used)
 - \odot for a system with n variables, there are n to 2n steps necessary to calculate the equilibrium geometry with ±0.001Å and ± 0.1° accuracy





Structures of molecules **Determination of equilibrium geometry** Calculating equilibrium binding distances is not enough. The relationship between calculated and measured parameters, possible errors and their causes should be carefully analyzed. r(C₁-C₂) r(C₁-F₄) $\alpha(C_1C_2F_5)$ $\alpha(F_6C_3F_7)$ (°)r(C₂-F_c) (mg) (pm) (pm) (pm) 128.4 HF/DZP 128.5 133.1 150.1 105.8 144.8 HF/TZ2P 144.6 128.0 128.3 133.0 149.8 MP2/DZP 132.2 146.9 131.0 135.7 150.0 105.7 MP2/TZ2P 146.5 131.2 130.8 135.6 149.8 105.8 ED 146.8(3) 131.4(8) 131.3(4) 135.6(3)

131.3(3) 135.8(3)

131.5(3) 136.1(4)

145.3(3) 129.6(4) 131.2(2) 137.0(2) 149.9(6) 105.4(5)

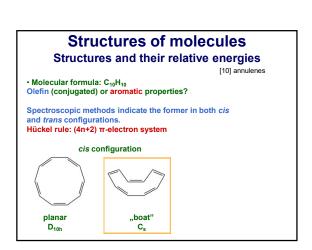
150.4(9) 105.4(5)

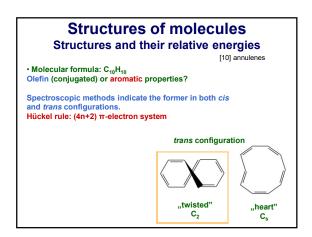
146.0(3) 131.0(8)

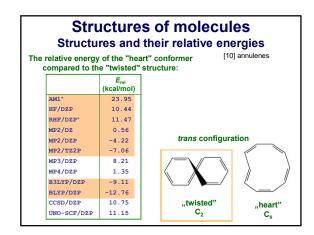
146.1(3) 130.7(13)

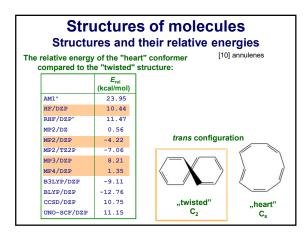
ED/MW/N

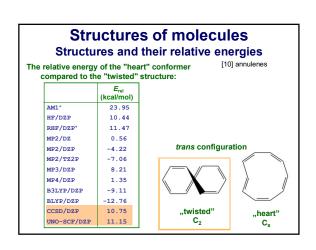
RD

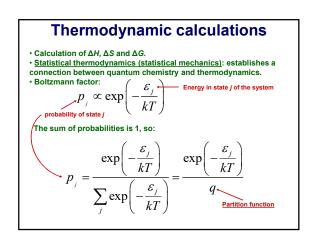


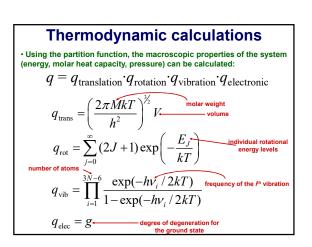












Thermodynamic calculations

• Using the partition function, the average energy of the system can also be calculated:

$$E_{\rm tot} = E_{\rm trans} + E_{\rm rot} + E_{\rm vib} + E_{\rm elec} + E_{\rm nucl.\ repulsion}$$

$$E_{\rm vib} = \sum_{i=1}^{3N-6} \left(\frac{h v_i}{2} + \frac{h v_i}{\exp(-h v_i / kT) - 1} \right)$$
 The zero point energy of the molecule

$$E_{\rm rot} = \frac{3}{2} NkT \ \mbox{(non-linear)}, \quad E_{\rm rot} = NkT \ \mbox{(linear)}$$

$$E_{\text{trans}} = \frac{3}{2} NkT \stackrel{\underline{\text{Sources of error:}}}{\bullet \text{ Coupling}} \text{ between differer} \\ \bullet \text{ Managing internal rotation}$$

Thermodynamic calculations

Using the gas law:

$$\Delta H = \Delta E + p\Delta V = \Delta E + \Delta nRT$$

Absolute entropy of the system:

$$S = S_{\text{trans}} + S_{\text{rot}} + S_{\text{vib}} + S_{\text{elec}} - nR \left[\ln(n \cdot N_0) - 1 \right]$$

$$S_{\text{trans}} = nR \left\{ \frac{3}{2} + \ln \left[\left(\frac{2\pi MkT}{h^2} \right)^{\frac{3}{2}} \left(\frac{nRT}{p} \right) \right] \right\}$$

$$S_{\text{rot}} = nR \left\{ \frac{3}{2} + \ln \left[\frac{(\pi v_{\text{A}} v_{\text{B}} v_{\text{C}})^{1/2}}{\sigma} \right] \right\}$$

Thermodynamic calculations

Using the gas law:

$$\Delta H = \Delta E + p\Delta V = \Delta E + \Delta nRT$$

Absolute entropy of the system:

$$S = S_{\text{trans}} + S_{\text{rot}} + S_{\text{vib}} + S_{\text{elec}} - nR \left[\ln(n \cdot N_0) - 1 \right]$$

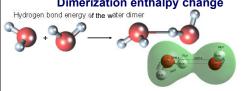
$$S_{\text{vib}} = nR \sum_{i} \left\{ \left[\left(h v_{i} / kT \right) \cdot e^{h v_{i} / kT} - 1 \right] - \ln(1 - e^{-h v_{i} / kT}) \right\}$$

$$S_{\text{elec}} = nR \ln g$$

• It is known from classical thermodynamics that:

$$\Delta G = \Delta H - T\Delta S$$

Thermodynamic calculations Dimerization enthalpy change



- In the first approximation, the dimeric bonding energy is the energy difference between the dimer and the two monomers
- The geometry can be calculated at a low level (e.g.: MP2).
- In the perturbation method, we only take into account the valence electrons, and we "freeze" the inner shells (frozen core method).
- Base-superposition error (BSSE, the same base for the monomer is different in "size" than for the dimer)
- · counterpoise (CP) method can be used to "offset" the effect

Thermodynamic calculations Dimerization enthalpy change Calculated: $\Delta E = -4.83 \text{ kcal/mol}$ RI-MP2/cc-pVxZ MP2/cc-pVxZ (CP corrected) RI-MP2/cc-pVxZ (CP corrected) MP2/aug-cc-pVxZ MP2/aug-cc-pVxZ (CP corrected) RI-MP2/aug-cc-pVxZ (CP corrected)

Thermodynamic calculations Dimerization enthalpy change

- More careful consideration of electron correlation (MP4 instead of MP2) results in an increase of energy only 0.05 kcal/mol.
- · Effect of zero point energy
- Effect of zero point energy
 Temperature increase from 0 K
 to the T of the measurement (375 K)
 Estimation of vibration anharmonicity
 Measured: $\Delta H = -3.6(5)$ kcal/mol
 Measured: $\Delta H = -3.6(5)$ kcal/mol
- $\Delta H = -3.2(1) \text{ kcal/mol}$

- Experimental difficulties increase the inaccuracy of the
- Careful analysis of calculations, consideration of relevant factors and effects improve the accuracy of the calculation

Chemical reactions

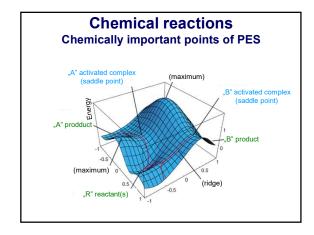
- There is limited experimental evidence of what is happening in a chemical process
 • (products, product ratio, reaction rate, rate constant)

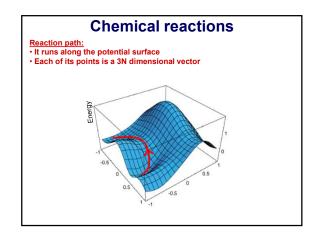
Assumption of reaction mechanism based on electrostatic properties. Calculation of the total energy (or ΔG) for reagents, products, intermediates, transition states. Calculation of the full PES.

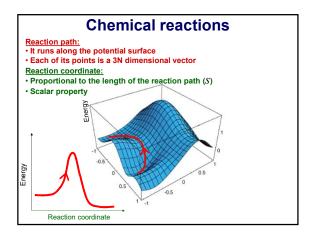
Chemical reactions Chemically important points of PES **Minima** The individual molecules, stable conformers can be assigned to them. First derivatives (gradients) are 0, second derivatives are positive. There are global (reactant, product) and local minima (intermediate). The "depth" of the minima sets the relative thermodynamic stability of

Chemically important points of PES • Saddle points belong to the activated complexes of the reactions (or conformational changes). • Gradients are 0, second derivatives are negative except for one. • The "hight" of the saddle point sets the rate (kinetics) of the reaction.

Chemical reactions







Chemical reactions

- Reaction path:
 It runs along the potential surface
 Each of its points is a 3N dimensional vector
 Reaction coordinate:
 Proportional to the length of the reaction path (S)
- Scalar property
- Scalar property $\text{- Displacement along the reaction path:} \\ \mathrm{d}s^2 = \sum_{i=1}^{3N} \left(\mathrm{d}q_i\right)^2$ The ℓ^{p} coordinate of a point on the reaction path

The ℓ^{th} coordinate of a point on the reaction pauli η is Direction of reaction path: $\eta = \frac{\mathrm{d} q(s)}{\mathrm{d} s} = \sum_{i=1}^{3N} \left(\frac{\mathrm{d} q_i}{\mathrm{d} s}\right) \mathbf{e}_i$ unit vect

• "Curvature" of the reaction path: $\mathbf{K}(s) = \frac{\mathrm{d}^2 \mathbf{q}}{\mathrm{d}s^2}$

